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# Data Representation, Logic, Huffman Coding, Binary Numbers 

DUE: $3: 30 \mathrm{pm}$ (start of class) Monday November, $30^{\text {th }}$. Please staple all sheets together BEFORE class.

Goal: The purpose of this assignment is to get a little practice with binary numbers, think about representing data digitally, and review basic logic as the foundation of how computers compute.

## Exercises:

## Binary Numbers

1 Convert 10 base 10 to base 2 . $\qquad$
2 Convert 16 base 10 to base 2 . $\qquad$
3 Convert 32 base 10 to base 2 . $\qquad$
4 Convert 217 base 10 to base 2. $\qquad$
5 Convert RGB color $(128,0,255)$ to base 2 . $\qquad$ , $\qquad$ , $\qquad$ )
6 Add 1101011 base 2 to 1011100 base 2, SHOW YOUR WORK.
7 Add 1011 base 2 to 110 base 2. SHOW YOUR WORK.

$$
\begin{array}{rr}
1101011 & 1011 \\
+1011100 & +110 \\
\hline
\end{array}
$$

8 What letters does this binary (base 2) data correspond to assuming it is in ASCII? $01001010,01100001,11110111,00110000=$ $\qquad$ , $\qquad$ , $\qquad$ ,

| ASCII | $\begin{aligned} & 0 \\ & 0 \\ & 0 \\ & 0 \end{aligned}$ | $\begin{aligned} & 0 \\ & 0 \\ & 0 \\ & 1 \end{aligned}$ | $\begin{aligned} & 0 \\ & 0 \\ & 1 \\ & 0 \end{aligned}$ | $\begin{aligned} & 0 \\ & 0 \\ & 1 \\ & 1 \end{aligned}$ | $\begin{aligned} & 0 \\ & 1 \\ & 0 \\ & 0 \end{aligned}$ | $\begin{aligned} & 0 \\ & 1 \\ & 0 \\ & 1 \end{aligned}$ | $\begin{aligned} & 0 \\ & 1 \\ & 1 \\ & 0 \end{aligned}$ | $\begin{aligned} & 0 \\ & 1 \\ & 1 \\ & 1 \end{aligned}$ | $\begin{aligned} & 1 \\ & 0 \\ & 0 \\ & 0 \end{aligned}$ | $\begin{aligned} & 1 \\ & 0 \\ & 0 \\ & 1 \end{aligned}$ | $\begin{aligned} & 1 \\ & 0 \\ & 1 \\ & 0 \end{aligned}$ | $\begin{aligned} & 1 \\ & 0 \\ & 1 \\ & 1 \end{aligned}$ | $\begin{aligned} & 1 \\ & 1 \\ & 0 \\ & 0 \end{aligned}$ | $\begin{aligned} & 1 \\ & 1 \\ & 0 \\ & 1 \end{aligned}$ | $\begin{aligned} & 1 \\ & 1 \\ & 1 \\ & 0 \end{aligned}$ | 1 1 1 1 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0000 | Nu | $\mathrm{s}_{\mathrm{H}}$ | $s_{x}$ | ${ }^{\mathrm{E}} \times$ | $\mathrm{E}_{\mathrm{T}}$ | $\mathrm{E}_{\mathrm{o}}$ | $A_{K}$ | $\mathrm{B}_{\mathrm{L}}$ | ${ }^{\text {B }}$ | $\mathrm{H}_{T}$ | $L_{\text {F }}$ | ${ }^{\text {r }}$ | $\mathrm{F}_{\mathrm{F}}$ | $\mathrm{c}_{\mathrm{R}}$ | $\mathrm{s}_{0}$ | $\mathrm{s}_{1}$ |
| 0001 | $\mathrm{D}_{\mathrm{L}}$ | $\mathrm{D}_{1}$ | $\mathrm{D}_{2}$ | $\mathrm{D}_{3}$ | $\mathrm{D}_{4}$ | $\mathrm{N}_{\mathrm{K}}$ | $s_{v}$ | $\mathrm{E}_{\mathrm{E}}$ | $\mathrm{c}_{\mathrm{N}}$ | $\mathrm{E}_{\mathrm{M}}$ | $\mathrm{s}_{\mathrm{B}}$ | $\mathrm{E}_{\mathrm{c}}$ | $\mathrm{F}_{\text {s }}$ | $\mathrm{G}_{\mathrm{s}}$ | $\mathrm{R}_{\text {s }}$ | $u_{s}$ |
| 0010 |  | ! | " | \# | \$ | \% | \& | ' | ( | ) | * | $+$ | , | - | . | $/$ |
| 0011 | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | : | ; | < | $=$ | $>$ | ? |
| 0100 | @ | A | B | C | D | E | F | G | H | I | J | K | L | M | N | O |
| 0101 | P | Q | R | S | T | U | V | W | X | Y | Z | [ | $\backslash$ | ] | $\wedge$ | - |
| 0110 | - | a | b | C | d | e | f | 9 | h | i | j | k | 1 | m | n | $\bigcirc$ |
| 0111 | P | q | r | S | t | u | V | W | X | Y | Z | \{ | \| | \} | ~ | $\mathrm{D}_{\mathrm{T}}$ |
| 1000 | ${ }_{0}$ | ${ }^{8} 1$ | $8_{2}$ | ${ }^{8}$ | ${ }^{\text {I }}$ N | $\mathrm{N}_{\mathrm{L}}$ | $\mathrm{s}_{\mathrm{s}}$ | $\mathrm{E}_{\text {S }}$ | $\mathrm{H}_{\text {s }}$ | $\mathrm{H}_{3}$ | $\mathrm{r}_{\text {s }}$ | $\mathrm{P}_{\mathrm{D}}$ | $\mathrm{P}_{\mathrm{v}}$ | ${ }_{\text {R }}$ | $\mathrm{s}_{2}$ | $\mathrm{s}_{3}$ |
| 1001 | ${ }^{\text {d }}$ c | $\mathrm{P}_{1}$ | $\mathrm{P}_{\mathrm{z}}$ | $\mathrm{S}_{\mathrm{E}}$ | $c_{c}$ | $M_{M}$ | $\mathrm{s}_{\mathrm{p}}$ | $\mathrm{E}_{\mathrm{p}}$ | $\mathrm{o}_{8}$ | $\mathrm{o}_{0}$ | $\mathrm{a}_{\text {A }}$ | $\mathrm{c}_{\text {s }}$ | $\mathrm{s}_{\mathrm{T}}$ | $\mathrm{o}_{\text {s }}$ | $\mathrm{P}_{\mathrm{M}}$ | $A_{P}$ |
| 1010 | ${ }^{\text {a }}$ O | i | ¢ | £ | ¢ | $¥$ | I | § | $\cdots$ | (c) | $0^{*}$ | " | $\neg$ | - | (R) | - |
| 1011 | - | $\pm$ | 2 | ${ }^{3}$ | - | $\mu$ | 4 | - | , | 1 | - | " | 1/4 | 1/2 | 3/4 | $\dot{\text { ¿ }}$ |
| 1100 | A | Á | A | A | Ä | Å | 厌 | Ç | E | É | $\hat{E}$ | E | 亡 | Í | $\hat{I}$ | İ |
| 1101 | Đ | N | ○ | $\bigcirc$ | Ô | O | Ö | $\times$ | $\varnothing$ | Ù | U' | Û | Ü | Y' | P | $\beta$ |
| 1110 | à | á | â | ã | ä | å | æ | Ç | è | é | ê | ë | i | í | î | 1 |
| 1111 | б | n | ò | ó | ô | õ | ö | $\div$ | $\varnothing$ | ù | ú | û | ü | ý | P | y |

Name: $\qquad$

## Logic

9 Complete the following truth tables.
(a) NOT $(p$ OR $q$ )

| $p$ | $q$ | $p$ OR $q$ | NOT $(p$ OR $q)$ |
| :---: | :---: | :--- | :--- |
| 1 | 1 |  |  |
| 1 | 0 |  |  |
| 0 | 1 |  |  |
| 0 | 0 |  |  |

(b) $p$ AND (NOT $q$ )
(c) $p$ AND $q$ AND $r$

| p | q | r | $p$ AND $q$ | $(p$ AND $q$ ) AND $r$ |
| :--- | :--- | :--- | :--- | :--- |
| 1 | 1 | 1 |  |  |
| 1 | 0 | 1 |  |  |
| 0 | 1 | 1 |  |  |
| 0 | 0 | 1 |  |  |
| 1 | 1 | 0 |  |  |
| 1 | 0 | 0 |  |  |
| 0 | 1 | 0 |  |  |
| 0 | 0 | 0 |  |  |


| p | q | NOT $q$ | $p$ AND (NOT $q$ ) |
| :--- | :--- | :--- | :--- |
| 1 | 1 |  |  |
| 1 | 0 |  |  |
| 0 | 1 |  |  |
| 0 | 0 |  |  |

10 Using the 3 basic logic gates shown here, draw logic diagrams for the following logical statements.

| $-\infty$ | OR | NOT |
| :---: | :---: | :---: |
| AND | OR |  |

a $\operatorname{NOT}(\mathrm{P}$ OR Q)
b (A OR B) AND (NOT C)
11 Write the logical statement that corresponds to the following logic diagram.


Name:
Huffman Coding (Please attach a separate sheet of paper for the Huffman trees.)
12
a Generate a binary Huffman tree from the following letter frequencies for the word bananarama.

| letter | b | a | n | r | m |
| :---: | :---: | :---: | :---: | :---: | :---: |
| frequency | 1 | 5 | 2 | 1 | 1 |

b Using the binary Huffman tree you created for (a), give the binary Huffman encoding for the letter sequence barn.

13
a Generate a binary Huffman tree from the letter frequencies in the tongue twister: She sells sea shells by the seashore. Do not include the space character in your tree.
b Using the binary Huffman tree you created for (a), give the binary Huffman encoding for the letter sequence share. $\qquad$
14 Create the Huffman tree that goes with the following frequency table.

| letter | c | s | r | t | e |
| :---: | :---: | :---: | :---: | :---: | :---: |
| frequency | 1 | 2 | 3 | 4 | 7 |

